## V.

> An Account of the Measurement of an Arc on the Meridian on the Coast of Coromandel, and the Length of a Degree deduced therefrom in the Latitude $12^{\circ}{ }^{\circ} 3^{\prime}$.

By Brigade Major william lambTON.

IN a former Paper which I had the honour to communicate to the Asiatick Society, I gave a short pketch of an intended plan for establishing a series of connecting points commencing from the Coromancel Coast, and extending across the Peninsula; but that Paper was only meant to convey a general jdea of the principles on which the work was to be conducted; a more circumstantial and scientific account, it was thought, would be more to the purpose, when I had the means of putting the plan in execution, and detailing the particulars. Since that time I have received a most complete apparatus, which has enabled me to proceed on the scale I originally proposed, and what is here offered is the beginning of that work, being the measurement of an arc on the meridian, from which is deduced the length of a degree for the latitude $12^{\circ} 32^{\prime}$ which is nearly the midd lle of the arç.

The triangles here mentioned are those only, from which the arc is obtained, and the base line, the foundation to the whole, is a measured line near the Seq Coast, an accqunt of which is here subjoined.

SECTION I. An accoùnt of the Basb Line.
Some time had been taken up in examining the country best suited for this measurement, and at length a tract was found near St. Thomas's Mount, extremely well adapted for the purpose, being an entire flat, without any impediment for near eight miles, commencing at the raee ground, and extending southerly. This being determined on, : and the necessary preparations made, it was begun on the 10th of April, and completed on the 22nd of May, 1802.

I had expected a small transit instrument from England, for the purpose of fixing objects in the alignement, and for taking elevations and depressions at the same time; but that instrument not having arrived, I thought it unnecessary to wait, particularly as the ground was so free from asceents and descents; I therefore used the same apparatus as I had formerly done, viz. the transit circular instrument and the levelling telescope fixed on a tripod with an elevating screw in the center. In all horizontal directions, this telescope fully answers the purpose, and as there has been no deviation from the level to exceed $26^{\prime} 30^{\prime \prime}$ excepting in one single chain, and those cases but very few, I feel entirely satisfied as to the accuracy of the whole measurement.

The chain which was made use of is the one I formerly had, and I was fortunate enough ta receive another from England, made also by the late Mr. Ramsden, and this having been measured of by the standard in London, when the temperature was $50^{\circ}$ by Fahrenhit's thermometer, it afforded me an advantage of correcting for the effects of expansion, a circumstance in which I was by no means satisfied in the former measurement. In order, therefore, to have a standard at all times to refer to, I bave reserved the new chain for that purpose, and used the

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old one only as à measuring chain, by which means I can always determine the correction for the wear.
By referring to the annexed table, it will appear that there are only four angles of depression, and two of elevation, taken in the whole length of the base; the rest are all horizontal measurements, and many of them consist of a great number of feet before it became necessary either to sink or elevate the coffers; when that was done, great care was taken to mark the termination of the preceding measurement; and for that purpose a small tripod was used in the shape of a T, with three iron feet to run into the ground, the straight side of which $T$ was placed in the line. Another small t was made with its top also parallel to the line, and fixed upon the large one so as to slide to the right or left, and upon that again was a long piece of brass made to slide out at right-angles to the top of the T ; in the middle of this brass a mark was made, which was brought to a plumb line let fall from the arrow, and the height from the brass to the arrow was noted down; when the succeeding chain was laid, which was to commence the new level or hypothenuse, the arrow was then brought, so that a plumb line freely suspended, would coincide with the mark on the brass slider. The height of that chain above the brass was likewise taken, by comparing those two heights the elevation or depression of the new commencement was determined, and those differences noted in the seventh and eigth columns of the table. The differences of the two aggregates contained in those columns, when applied to the ascents and descents, will therefore shew how much one extremity of the base is above the other. The height of the chain at the commencement and termination of the whole was of course taken from the ground.

All the other particulars respecting this measurement are nearly the same as that in the Mysore coun-
try, a full account of which has been published in a former volume of the Asiatic Researches. Some little alterations have been made in the coffers; that is, they were all of the same length, and the whole together about ninety-six feet, so as to give room for the pickets with the brass register heads. Their sides continued to the ends, and their depth on each side was the same, for the purpose of being turned every day that they might fall into a curve by their own weight and that of the chain. I also used tripods with elevating screws in the center, for supporting the coffers, making no other use of pickets than for the drawing and weight posts, and for carrying the register heads. The top of each stand on tripod was 2 thick circular piece of wood fixed firmly to the end of the elevating screw, and a slip of board was fastened across the circular top, screwed into the center, and allowed to turn round. When the ends of two coffers were placed on the top piece, this slip of board was admitted into the under part of each, and prevented their sliding off, a precaution that was very necessary on account of the high winds.
The point of commencement of the base was had by dropping a plummet, from the arrow of the chain suspended by a silken thread. A long but small bamboo picket had been driven into the ground till its top was level with the surface, and the cavity of the bamboo was such as just to receive the plummet, and when the first chain was in the coffers, drawn out by the weight at the opposite end, it was adjusted by the finger screw at the drawing post in such a manner that the plummet might hang suspended over. the cavity of the bamboo, while the thread was apphed to the arrow. This was done within the observatory tent, that the plumb line might hang freely without being disturbed by the wind. .The bamboo picket was preserved with great care during the time I was observing for the latitude, and was then pro-

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tected under the frame of the zenith sector. When the tent was removed, a large bamboo flag-staff was erected, whose cavity covered the picket, and in that state it remained until the measurement was completed.

At the termination of the base, being the end of a chain, one of the large hooped pickets was driven into the ground till its top was on a level with the coffers and under the arrow of the chain. The opposite end being adjusted by the finger screw, the arrow at the leading end was nearly the center of the picket. A mark was made, and a small round headed nail was driven in till it was level with the surface. The chain was again applied, and the arrow cut the center of the nail. The picket had been driven upwards of two and a half feet into very bard clay.

But that those extremities may be preserved, in case they may hereeafter be referred to, I erected small masses of hewn stone eight feet square at the bottom and four at the top, the axis of those masses being made to pass through the points of commencement and termination, and in order that this might be correctly done, the following method was used.

I marked ont the foundation of the building, so that the picket might be as nearly in the center of it as possible. The earth was dug about ä foot deep, reserving a space round the center untouched. After the foundation was brought to a level with the surface, the first tier of stones was laid, being one foot in height. The inner part was then filled up with stones and mortar, taking particular care at the same time that the center was not toucher. The next tier of stones was then laid, which was six feet square and one foot high. This also was filled in with great care, and some cement and bricks put gradually round the picket. After that the last tier was laid which was four feet square and also one foot high.

When these stones were firmly fixed small silken threads were drawn across each other in the diagonals of the square. A plummet (pointed) was then suspended from the point of intersection of those threads, and they were so moved that the point of the plummet coincided with the center of the nail in the picket. The position of these threads being determined, marks were inserted in the stone. The cavity was then filled up, and a square thick stone was fixed in the middle of the mass, having a circular place of about four inches diameter, sunk half an inch deep, and whose center was marked by a point. This point, by moving the stone and again applying the silken threads was brought to coincide with the point of intersection, and then it was firmly fixed and pointed.
Precisely the same kind of building was erected at the beginning of the base, but in place of having a picket in the center, four large hooped ones were, driven into the ground, forming a square of about ten feet, the small bamboo picket being intended as the center. Silken threads were then drawn across from the diagonal pickets, and so moved, that the plummet first used, suspended from the point of intersection of the threads, might drop into the cavity of the bamboo. That being adjusted, lines were drawn on the tops of the pickets where the threads had been extended. The building was then erected, and the center both of the second and last tier, was marked by the intersection of those threads when applied to the marks on the pickets.

Such has been the mode of defining the extremi-. ties of the line. The buildings are well built of stone and some brick, and will remain for years, if not injured by acts of violence. They are intended to receive an instrument on the top, and the points are points of reference if it should ever be thought. necessary to have recourse to them.

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 expansion of the Chains and their COMPARATIVE LENGTHS.As I wished to be satisfied with respect to the expansion of each of the chains, and their comparative lengths, I made a course of experiments for both purposes. I had accordingly the coffers arranged near the ground, that the drawing and weight posts might be driven deep and firmly fixed. Both the chains were then put into the coffers, and the comparisons made as follows :
April 10, at six P. M. the temperature by a mean of five thermometers was $85^{\circ}, 6$.
Three comparisons were made, and the old chain exceeded the new one, nine divisions of the micrometer screw.

April io, at six A. M. the temperature by a mean of five thermometers was $79^{\circ}$.
Four comparisons were made, and the old chain exceeded the new one nine divisions. Therefore at the commencemont, the old chain exceeded the new one in length, nine divisions of the micrometer.

May 23. After the base was completed, the temperature by a mean of five thermometers, was $86^{\circ}$.
By a mean of five comparisons, the old chain exceeded the new one 10,65 divisions.
24. The temperature by a mean of five thermometers was $84^{\circ}$.
And a mean of six comparisons, gave the excess of the old chain above the new one - - 11,08 do.
25. The temperature was $87^{\circ}$.

And a mean of two com$\underset{\text { Mean }}{\text { parisons, gave }}-\frac{11,00 \text { do. }}{10,86}$ do.

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Hence it appears, that at the conclusion of the base, the old chain was longer than the new one, 11 divisions of the micrometer very neatly, so that it had increased from being in use, 2 divisions, or $\frac{2}{208}$ inches.

These experiments were made with great attention, and when either chain was stretched out by the weight, it was carefully brought into a line in the coffers.

As I had reserved the new chain for a standard, and knowing the temperature at which it had been measured off in London, 1 considered it an object to determine its rate of expansion and contraction compared with the thernomettrs which had been in use in measuring the base, since these were but com-: mon ones, and might probably differ from those made use of by General Roy and others, who had determined the expansion of metals by the pyrometer; and I was further induced to do this, from seeing the great variation among them, when the degree of heat became above one hundred, which it generally was in the coffers every day before I left off. To avoid those irregularities arising from the expansions being checked by the resistance from the, pressure on the coffers, I chose the times of sunrise, and from one to two o'clock, P. M. for making the obserrations. Sunrise in India is generally the coolest time of the twenty-four hours, and the chain had during the night, on account of the uniform state of temperature, full time to free itself from any resistance. At the hottest part of the day likewise there is a considerable time when the thermometers are nearly stationary, which will afford time for the resistance in the coffers to be overcome, and it is.necessary to pay particular attention to this circumstance, for the chain will be perceived to lengihen often for nearly balf an hour after the thermometers are at their highest.

I had made a great many experiments prior to the measurement, but found great irregularity, partly from not attending sufficiently to the above circumstance, and partly from the unsteadiness of the drawing post, notwithstanding it was driven deep into very hard ground, and secured, as I thought, by having large stones pressed close on each side of it. To remedy this latter inconvenience, I had a staple driven into a brick wall, into which the iron was fixed with the adjusting screw for the chain, after which I perceived a perfect coincidence with the arrow and mark on the brass head, except what arose from the trifling expansion and contraction of the iron which held the chain. I then began a new course of experiments on both the chains, and the results were as fol-lows:-

Experiments for determining the expansion of the new Chain.

| $180 \%$. <br> -Month. | TIME. |  |  |  | Total expansion and contraction. | Total due to $1^{\circ}$ | REMARKS. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| June 4.2 | 2 P.M. | .116,4 | 33,4 |  | Inches. | Inches. | Weather |
|  |  |  |  | 51 | ,245157 | ,00734 |  |
|  | 0 rise. | 83 | 40,8 | 64 | ,207648 | ,00754 | clear ond |
|  | 2 P.M. | 123,8 82,5 | 41,3 | 64 | ,307648 | ,00744 | windy |
|  | O rise. | 82,5 80 |  |  |  |  | during |
|  | 2 P.M. | 119,1 | 39,1 | 60 | ,288420 | ,00737 | the whole |
|  | O rise. | 119,1 81,4 | 37,7 | 57 | ,273999 | ,00727 | of these |
|  | 2 P.M. | 81,4 | 40,5 | 63 | ,302841 | ,00747 | experi- |
|  | $\bigcirc$ rise. | 121,9 79,7 | 42,2 | 66 | ,317262 | ,00752 | ments. |

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Experiments for determining the expansion of the old Chain.

| $\underbrace{1802 .}_{\text {Month. }}$ | TIME. |  |  |  |  | $\begin{aligned} & \text { Total } \\ & \text { due to } \\ & 1^{\circ} \end{aligned}$ | REMARES |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| June 8. | $\bigcirc$ - rise. |  | 26,8 |  |  |  | Cloudy weather and high winds during the whole of these experiments. |
|  | ${ }_{2}^{2} \mathbf{P} \mathbf{P}_{1} \mathrm{M}_{4}$ | 110,3 | 25, | 40 | ,2018944 | ,00766 |  |
|  | $\begin{aligned} & 0 \\ & 1 \\ & 1 \end{aligned} \mathbf{~ r i s e} \mathbf{~ M}$ | ${ }^{85,2}$ | 24,8 | 39 | ,187473 | ,00755 |  |
|  | $\bigcirc$ | 80,2 |  |  | . 201894 | ,00724 |  |
|  | L P.M. | 108,1 | 27,9 24,8 | 48 | ,2182666 | ,00724 |  |
|  | $\bigcirc$ rise. 2 P.M. | 83,3 | 24,8 28 | 38 | \|r 21818964 | ,00721 |  |
|  |  | $\begin{gathered} 111,3 \\ 80 \end{gathered}$ | 31,3 | 46 | ,221122 | ,00706 |  |

It appears from these results, that the expansion due to $1^{\circ}$ of the thermometer is less than what has been allowed by experiments made in England, but this might arise from the thermometers, as they were such as could be purchased in the shops, and therefore most probably of the best kind. Great care, bowever, was taken to watch the moment when they stood the highest, and though they varied from one another considerably at that time, yet that variation was generally the same in equal temperatures.

The reductions from the hypothenuses to bring them to the horizontal level, were made by numbering the feet from the old chain as they were measured, viz. by calling 32 chains 3200 feet, which would be 3800,115 feet by the new chain; but this would produce no sensible error in the versed sign of a very small angle, and on that account these decimals were not taken into the com-
putation, which was thought less necessary, since the whole deduction did not amount to three inches. Neither was any notice taken of the different heights of the hypothenuses or levels one above another, as that difference was too trifling to affect a length of thirty or forty chains. The base has therefore been considered at the same distance from the center of the earth, before it was reduced to the level of the sea, and the perpendicular height of the south extremity, which I have considered as nearly the general height, has been taken for that purpose. That perpendicular height was obtained by comparing the south with the north extremity, and the height of the latter was determined by observations made at the race-stand and on the sea-beach, where allowance has been made for the terrestrial refraction. The following is the manner in which it has been determined:

On the top of the race-stand, the under part of the flag on the beach was observed to be depressed $9^{\prime} 30^{\prime \prime}$; and at the beach, the top of the race-stand was elevated $7^{\prime} 15^{\prime \prime}$. When the instrument was on the platform of the race-stand, the axis of the telescope was on a level with the top of the railing, which was observed from the beach. But at the beach the axis of the telescope was four feet below the part of the flag which had been observed.

The horizontal distance from the station on the stand to that on the beach is $=19208$ feet. Then as $19208: 4::$ Rad : tan. $43^{\prime \prime}$, which must therefore be added to the observed depression of the flagHence $9^{\prime} 30+43^{\prime \prime}=10^{\prime} 18^{\prime \prime}$ is the depression of the axis of the telescope on the beach, observed from the race-stand.

Now the station on the beach is nearly at right angles to the meridian, therefore, by allowing L 2

60957 fathoms to the degree, 19208 feet will give an arc of $3^{\prime} 9^{\prime \prime}$ very nearly, which is the contained aro. And the difference between the depression and elevation being $2^{\prime} 58^{\prime \prime}$, we have $\frac{3^{\prime} 0^{\prime \prime}-0^{\prime} \cdot 5 s^{\prime \prime}}{\sigma}=5^{\prime \prime}, 5$ for the terrestrial refraction. Hence, since the observed elevation of the stand, plus half, the contained arc would give the angle subtended by the perpendicular height of the stand above the telescope at the beach, were there no refraction, we shall have $7^{\prime} 15^{\prime \prime}+\frac{3^{\prime} n^{\prime \prime}}{g^{\prime \prime}}-5^{\prime \prime}, 5=8^{\prime} 44^{\prime \prime}$ for the true angle sabtended by the perpendicular height, which being taken as tangent, to the horizontal distance and radius, we have $\mathrm{R}: \tan .8^{\prime} 44^{\prime \prime}:: 19208:$ 48,797 feet the height required. But the axis of the telescope on the beach was determined by levelling down to the water, to be 21,166 feet above the sea. Which, added to the above, give 69,963 feet for the perpendicular height of the top of the stand above the level of the sea.

Now the top of the race-stand was determined by levelling to be 31,25 feet above the northextremity of the base; which taken from the other, leaves 38,713 for the north extremity of the base above the sea, which extremity being, by the table, 22,96 feet above thie south extremity, we shall have 15,753 feet from the perpendicular height of the south extremity of the line above the level of the sea; and from this height the length of the base has been reduced.

The angles of elevation and depression were taken by the circular instrument, from a mean of several observations, and the error of collimation was corrected by turning the transit over, and the horizontal plate half-round. But the weather was rather dull during the whole of these operations.

## TABLE.

Containing the particulars of the measurement of a.base line near St. Thomas's Mount, commencing in latitude $18^{\prime \prime}, 00^{\prime}, 29^{\prime \prime}, 59 \mathrm{~N}$. and extenđing 40006,4418 feet South Westerly, making an angle with the meridian $0^{\circ} 10^{\prime} 36^{\prime \prime}$. The first column contains the number of the hypathenuse, or measured distances. The second the length of each in feet. The third the angles of elevation and depression (which each hypothenuse makes with the horizon). The fourth the quantities to be subtracted from the respective hypothenuse to reduce it to the horizon. The fifth the perpendicular ascents and descents to each hypothenuse. The sixth the commencement in inches of every hypothenuse above or below the termination of the one preceding; and the seventh contains the mean temperature during the respective measurement.

|  |  | Angles of elevation and depreaso | Dedncti: ons from eact hy: potho | Perpendicuiar. |  | Comineitce-ment from the last. |  |  | REMARES. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bide id |  |  | Ascents. | Descents. | $\begin{array}{\|c\|} \hline \text { above } \\ \text { Inch. } \end{array}$ | $\begin{aligned} & \text { belinw } \\ & \text { laches. } \end{aligned}$ |  |  |
|  |  | - |  |  |  |  |  |  |  |
| 1 | 6000 | 01940 | ,00984 |  | 3,4393 | 25,5 |  | 86,6 | Commenced |
| 2 | 5000 | 02600 | 430 |  | 3,781, ${ }^{\text {a }}$ |  |  | 81,9 | the 10th |
| 3 | 21000 | 02630 | ,0<́237 |  | 10,18i 8 | 2,5 |  | 84,5 | April, 1802. |
| 4 | 300 | Level. |  |  |  | 2,37 |  | 94,5 |  |
| 5 | 600 | do. |  |  |  |  | 7,37 | 84 |  |
| 6 | 100 | do. |  |  |  | 2,75 |  | 90,4 |  |
| 7 | 400 | do. |  |  |  | 5,75 |  | 95,3 |  |
| 8 | 500 | do. |  |  |  | 1,12 |  | 62, 2 |  |
| 9 | 100 | do. |  |  |  | 5,0 |  | 91 |  |
| 10 | 400 | do. |  |  |  | 4,0 |  | 93,2 |  |
| 11 | 300 | do. |  |  |  |  | 7,25 | 93,3 |  |
| 12 | 3000 | 02080 | ,00534 |  | 1,7890 |  | 8,25 | 84,9 |  |
| 13 | 100 | 1. vel. |  |  |  |  | 10,0 | 90 | Tiu the water. |
| 14 | 1003 | 30230 | ,14088 | 53062 |  |  | 8,5 |  | $\}^{\text {Eank of } 2}$ |
| 15 | 100 | Level. |  |  |  | 8, |  | 107,4 | \} Tank. |

MEASUREMENT OF AN ARC ON THE

|  |  | $\begin{aligned} & \text { Angles of } \\ & \text { eierations } \\ & \text { aur de. } \\ & \text { pressions. } \\ & - \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { Deducti- } \\ & \text { ens from. } \\ & \text { each hy- } \\ & \text { pothen. } \end{aligned}$ | Perpendicular. |  | Commencement from the last. |  |  | REMARKS. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Ascents | Descents. | above Inches. | helow Inches. |  |  |
| 16 | 100 | $\begin{aligned} & 0 \\ & \text { Level. } \end{aligned}$ |  |  |  |  | 40,87 | 105,8 |  |
| 17 | 200 | do. |  |  |  |  | 11,75 | 82,2 |  |
| 18 | 200 | do. |  |  |  |  | 14,12 | 83,4 |  |
| 19 | 500 | do. |  |  |  |  | 6,12 | 89,2 |  |
| 20 | 306 | do. |  |  |  |  | 5,25 | 92,9 |  |
| 21 | \%00 | do. |  |  |  | 12,25 |  | 87,5 |  |
| 22 | 300 | do. |  |  |  |  | 7,87 | 93,7 |  |
| 23 | 500 | do.*. |  |  |  |  | 17,5 | 92,8 |  |
| 24 | 900 | do. |  |  |  |  | 10,12 | 91,2 |  |
| 25 | 400 | do. |  |  |  |  | 4,75 | 85,8 |  |
| 26 | 500 | do. |  |  |  |  | 10,62 | 85,8 |  |
| 27 | 300 | do. |  |  |  |  | 11 | 93,5 |  |
| 28 | 400 | do. |  |  |  |  | 12 | 86,8 |  |
| 29 | 1200 | do. |  |  |  |  | 11,37 | 88,9 |  |
| 30 | 600 | do. |  |  |  | 3,5 |  | 86,7 |  |
| 31 | 1700 | do. |  |  |  | 9,37 |  | 90,6 | The 2 chain |
| 32 | 700 | do. |  |  |  | 4 |  | 85,4 | in the |
| 33 | 200 | do. |  |  |  | 10,75 |  | 91,3 | Chingle- |
| 34 | 800 | do. |  |  |  | 7,5 |  | 91,5 | pet road. |
| 35 | 400 | do. |  |  |  |  | 12,75 | 94,8 |  |
| 36 | 2000 | do. |  |  |  |  | 15 | 90 |  |
| 37 | 2100 | do. |  |  |  |  | 6,9 | 91,5 |  |
| 38 | 32000 | 00450 | ,00320 | 4,4991 |  | 8,8 |  | 90,1 |  |
| 39 | 900 | Level. |  |  |  |  | 1,8 | 96,9 |  |
| 40 | 1200 | do. |  |  |  |  | 11,4 | 90,5 |  |
| 41 | 800 | do. |  |  |  |  |  | 93,7 |  |
| 42 | 1400 | do. |  |  |  |  | 6,7 | 93,4 |  |
| 43 | 1100 | do. |  |  |  |  | 2,8 | 90,9 |  |
| 44. | 500 | do. |  |  |  |  | 3 | 93,4 |  |
| 45 | 600 | do. |  |  |  | 2 |  | 88,7 |  |
| 46 | 1200. | do. |  |  |  | 10,2 |  | 93,8 |  |
| 47 | 3200 | do. |  |  |  | 7,2 |  | 93,1 |  |
| 48 | 1400 | do. | . |  |  | 7,2- |  | 90,4. |  |
| 49 | 2200 | do. |  |  |  | 5,6 |  | 91,8 |  |
| 50 | 800 | do. |  |  |  | 7,3 |  | 97,3 | 2td May, |
|  | 40000 |  | ,23593 | 9,8053 | 25,1908 | 18i,16 | 272,06 | 90,8 |  |

North above the south extremity 22,96 feet in perpendicular height.

At the commencement, the old chain (with which the measurement was made) exceeded the new one by nine divisions of the micrometer, equal to $\frac{0.043465}{12}$ feet. Therefore $100 \pm \frac{0.04306 .3}{0.2} \times$ 400 will be the measures in lengths of the new chain, equal . . . . . . . . . . . . . . 40001, 4420

At the conclusion, the old chain exceeded the new one by eleven divisions, consequently it had increased by wear two divisions of the micrometer $=0,0008$ feet. Hence $\frac{9008}{2}$ $\times 400=0,1600$ feet, is the correction for the wear, which add $+0,1600$
Whence the apparent length of the base, will be 400,016020 lengths of the new chain,

40001, 6020
The sum of all the corrections in column fourth for obtaining the hor rizontal distances, is 0,2359 feet, which must therefore be deducted
$-0,2359$
And this will give the apparent horizontal length of the base, in terms of the new chain 400,013661 lengths, or

40001,36661
The mean temperature for the whole base is $90^{\circ}, 8$ and the new chain was measured off when the thermometer stood at $50^{\circ}$. hence to reduce the whole horizontal length to the standard temperature of $62^{\circ}$, the equation will be expressed by $\frac{(000,8-600) \times 0.0097-(620-300 \times 1001997}{18} \times$ 400,013661 feet, or 5,1162 feet which must be added, $+5,1162$
Hence the whole horizontal distance corrected for $62^{\circ}$ will be,

40006,4823
Which reduced to the level of the
sea will be, . . . . . . . . . . 40006,4418
L4

Note, the quantity,+ 0074 inches is the expansion of the chain due to $1^{\circ}$ of the thermometer as determined by my own experiments detailed in the annexed memoir. By General Roy's experiments with the pyrometer, it was,+ 00763 inches.

The quantity,+ 01237 inches is the expansion of 100 feet of brass due to $1^{\circ}$ of the thermometer.

By the experiments I made in the Mysore the expansion of the old chain was,+ 00725 inches due to $1^{\circ}$. By these experiments it is,+ 00737 inches, but I give the preference to the latter on account of the chains being fixed to the wall.

The radius of curvature for reducing the base to the level of the sea, is assumed at 3448748 fathoms being the radius to the meridional circle on which one degree is computed to be 60191 in the latitude of $13^{\circ}$.

Section II.-Observations for determining the Angle which the Base Line makes with the Meridian.

At the North end of the base latitude . . . . . . . . . . . $13^{\circ} 00299^{\prime \prime}, 59 \mathrm{~N}$.
September 24th, on the evening the polar star when at its greatest Eastern elongation was observed to make an angle North Easterly with the base line produced
$1^{0} 35^{\prime} 08^{\prime \prime}, 7$
The apparent polar distance of the star at that time was $1^{\circ}$ $44^{\prime} 40^{\prime \prime} 2$ with which and the above latitude, the computed azimuth was, . . . . . . 14725,7

MERIDIAN OK THE COABT OF COROMANDEL. 153
Therefore the line whien produced Northerly will make an angle with the meridian North Easterly, . . . . . . . . . . . . . . . 0 12 17, 0
September 26 th, on the evening the angle North Easterly with the base line produced was, . . . 13513,1
The apparent polar distance on that day was, $1^{10} 44^{\prime} 39^{\prime \prime} 8$ which will give the azimuth, . . 14725,2
Therefore the angle between the line and meridian will be, . . . 0 12 12, 1
September 30th, on the evening the angle was observed, . . . . . . 1 35 06, 7
The apparent polar distance for that day being $1^{\circ} 44^{\prime} 38^{\prime \prime} 1$ the azimuth will be, . . . . . . . . . 147 99, 5
Hence the angle by this observation is, . . . . .. . . . . . . . . 0 12 16, 8

At the South end of the base-Latitude.

125352,8
October 7th. In the morning, the polar star when at its greatest western elongation, was observed to make an angle N. Westerly with the base line produced. . . 15936,9
The apparent polar distance at that time was $1^{\circ} 44^{\prime} 35,7$, and this with the above latitude will give the azimuth. . ...... 14718,9
Therefore the angle which this line produced, makes with the meridian North Easterly. . . . . 0 12 18, 7
And the mean of these four is . . $\quad 0 \quad 1216,15$
The last observation was made under the most favourable circumstances, it being just day light;
the flag-staff at the north extremity of the line was observed immediately after the star ; and the morning being perfectly clear, no unsteadiness or uncertainty arose from the effects of the vapour, which had occasioned the difference between the angles on the 24th and 26 th .

When the observation was made on the 90th, a blue light was fixed at the south end of the base.

Section III.-Commencement of the operations from the base. The large theodelite.

After the completion of the base line, there remained nothing of importance to be done until I received the large instrument, which arrived in the beginning of September. I had however made an excursion down the sea coast, as far as Poxdicherry, for the purpose of selecting the properest stations for determining the length of a meridional arc. This and the measurement of a degree at right-angles to the meridian I considered as the first object of this work: I accordingly lośt no time in proceeding to accomplish these desiderata.

The instrument above alluded to was made by Mr. Cary, and is in most respects the same as that described by General Roy in the Philosophical Transactions for the year 1790, with the improvements made afterwards in the microscopes, and in an adjustment to the vertical axis, by which the circle can be moved up or let down by means of two capstan screws at the top of the axis. These are mentioned in the Philosophical Transactions for 1795, in the account of the trigonometrical survey. By sinking the circle on the axis, it is better adapted for travelling, and when the microscopes are once adjusted to minutes and seconds,
on the limb of the instrument, the circle can always be brought back to the proper distance from them. Great attention however is necessary in bringing the axis down, so that the wires in each microscope being fixed at opposite dots on the limb, they may coincide with the same dots when the circle is turned half round, or made to move entirely round, and in a contrary direction to what it had -been moved before; which latter method has been recommended by the maker. This circumstance respecting the axis should be most scrupulously attended to before the adjustment of the micrometers begin, so that when by arranging the lenses in such a manner that ten revolutions of the micrometer may answer to ten minutes an the limb, and therefore one division to one second, the circle can always be brought to its proper height, by trying the revolutions of the micrometer.

It has however been found from experience, that unless in cases of very long and troublesome marches, it is not necessary to sink the axis. The carriage being performed altogether by men, there is not that jolting which any other mode of conveyance is subject to, and as I found, that a considerable time was taken up in adjusting the axis before the revolutions of the micrometers could be brought to their intended limits, I therefore laid it aside, unless under the circumstances above mentioned.

The semicircle of the transit telescope is graduated to $10^{\prime}$ of a degree in place of 30 , which was the case with the semicircle described by General Roy, and the micrometer to the horizontal microscope applied to this semicircle, making one revolution in two minutes, and five revolutions for ten minutes on the limb; and the scale of the micro-
meter being divided into sixty parts, each part is therefore two seconds of the circle.

A number of experiments have been made for determining the error of the semicircle, and to ascertain the place of, the fixed wire in the horizontal microscope, so as to divide the error. It has appeared in the event, that the telescope being in its right position, (that is, when the limb and microscope were on the left hand,) and the fixed wire placed at Zero on the semicircle, when the circle or limb of the theodelite was turned $180^{\circ}$ in Azimuth, and the telescope turned over, the fixed wire was then distant from Zero on the opposite part of the are by a mean of a great many observations $2^{\prime} 57^{\prime \prime}$, the half of which is therefore the error, This half was carefully set off from Zero by the moveable micrometer wire, and the fixed one brought to coincide with it. On the right appli, cation of this error, there will be $1^{\prime} 28^{\prime \prime}, 5$ to add to the elevations and subtract from the depressions. The observations for determining this quantity were repeated at different times, and under the most favourable circumstances; the adjustments of the whole instrument being frequently examined, and the level applied to the telescope, reversed at most of the observations. For the line of collimation, as these corrections depend on having a welldefined object, I fixed a bamboo upwards of a mile distant from the observatory tent, and tied round it several narrow stripes of black silk, one of which was near the horizontal wire when the axis of the telescope intersected the staff after being brought to a level by the bubble. Then the instrument being adjusted, and the telescope directed to the bamboo, being perfectly level, and the wire of the micrometer in the piece brought to the intersection of the cross wires, the angular distance to the
mark on the bamboo was measured by the runs of that micrometer, and the wire brought back to the point of intersection of the other wires. The circle was then turned half round and the telescope reserved or put again into the same Ys. The levelling adjustment was then made, and the angular distance from the intersection of the wires to the black mark again taken, half the difference between which and the former was of course the error of collimation. This error was repeatedly reduced till it became very small, half by the finger screw of the clamp to the semicircle, and half by the adjusting screws to the levelling rods. After that, the remaining error was repeatedly examined and found to be $2^{\prime \prime}, 96$ to be subtracted from the elevations and added to the depressions when the telescope is in the ordinary position, or when the semicircle and microscope are on the left hand; but vice versa when in the contrary position. These errors of the semicircle and line of collimation being opposite, the result from comparison will be, "That when elevations or depressions are taken with the semicircle, $1^{\prime} 26^{\prime \prime}$ must be added to the former, and subtracted from the latter."

And that when the elevations and depressions are taken by the micrometer in the eye piece $2^{\prime \prime}, 36$ must be deducted from the eleoations and added to the depressions.

The micrometer in the focus of the eye-glass of the transit telescope is the same in all respects as the one mentioned by General Roy, that is to say, the circle or scale is divided into one hundred divisions, and there is a nonius fixed to the upper part of the telescope, which defines the revolutions of the micrometer as far as ten for the elevations and ten for the depressions. The following experiments
have been made with the same marked bamboo, for ascertaining the value of these divisions, and it. has been found that seven revolutions and $61,4 \mathrm{di}$ visions are equal to ten minutes on the limb of the semicircle, so that one division is equal to ,788 of a second.

## TABLE

Of experiments for determining the valuation of the resolutions and divisions on the micrometer in the eye-piece of the telescope.

| Memath. | Micrometer Divisions. | $\begin{gathered} \text { No. of } \\ \text { se. } \\ \text { conds.' } \end{gathered}$ | Value of 1 Division. | Month. | Micrometer Divisions. | $\begin{gathered} \text { No. of } \\ \text { se- } \\ \text { coheds. } \end{gathered}$ | Value of 1 Division. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nov. 26. | $\mathbf{d}$ | 7835 | 0.78 | Nov. 26. | $\begin{gathered} d \\ 1000 \end{gathered}$ | 780 | 0 |
|  | 994 | 787 | 0,782 |  |  | 800 | 0,800 |
|  | 994 | 773 | 0,777 |  |  | 787 | 0,787 |
|  | 1005 |  | 0,783 |  |  | 794 | 0,794 |
|  | 1002 | 794 | 0,794 |  |  | 788 | 0,788 |
|  |  |  | 0.788 |  |  | 782 | 0,782 |
|  |  | ean | 0,788 |  |  | 788 | 0,788 |

Hence one second will be equal to 1,269 divisions. One minute . . . . . . . 75,72 ditto. Ten minutes . . . . . 757,2 ditto.

## SECTION IV.

Angles taken with the large theodelite between 97th September 1802, and 13th of April, 1803.
at the north end of the base.
Between
And
Observed Angles.
 Perumbauk hill, . . 0947 58,9
Perumbaulh hill, Mount station, . . . 8121 05,2

## meridian on the coast of coromandel. 150

## at the south end of the base.



## AT MULLAPODE HILL.

Between And Observed Angles.

Perumbauk hill; Coonoowaucum hill, 13929 07,8 $\left.\begin{array}{l}\text { Coonoorvaucum } \\ \text { hill, }\end{array}\right\}$ Munnoor station, . 8121 03,0 Tandray station, $\begin{gathered}\text { ditto, } \\ \text { Mungot station, }\end{gathered}$.

AT MUNNOOR STATION.


AT TANDRAY STATION.
Mungot station, Munnoor station, . 6018 30,7
Mullapode hill, . . . 270200,1
Munnoorstation, ditto, . . . . . 3316 20,8
Mullapode hill, Urrumbaucum hill, 9400 01,7 Poonauk hill, . . . . 8048 38,8

AT URRUMBAUCUM HILL.

Mullapode hill, | Tandray station, $\quad . .430250$ |
| :--- |
|  |
| Poonauk hill, . . . |
| 111 |
| 52 |
| 28,9 |

AT POONAUK HILL.
Mullappode hill, Urrumbaucum hill, 3925 15,6
Tandray station, . . 2713 47,4
Maumdoor hill, . . . 4919 0,46


AT PERMACOIL MILL.
Between And Obserged Angles.Woritty hill, Carrangooly hill, . . 420125,1Coomum hill, .... 1355100,0Coonum hilt, 1st flag on red nill, . 53 19 11,8Vellungcaud hill, Garrangooly, hill, .28 . 58 93,4New station on red hill, 98 29 08,8Chengcaud station,, : 4257 14,4
Mylum station, ditto $\quad$ ditto, : 29 29 41, \$at vellengeaud hill.
Permacoil hill, Carrangooly hill, . 11421 154 New station on red hill, $97 \quad 15 \quad 17,4$
at the new station on red hill.
Permacoil hill, Vellungcaud hill, ..... 441533,8 Mooratth station, . 992504,4吅: !
at mooratan btation.
$\left.\begin{array}{c}\text { Chengcaud sta- } \\ \text { qiont, }\end{array}\right\}$ Permacoil hill, ..... 8513 36,0
$\stackrel{\rightharpoonup}{c}$ Trioumdepoormom hill, ..... 6442 38,5
Ist Coomum hill, 1 st.flag on red hill, ..... 814830
Chengcaud station, ..... 543315
New station on Permacoil hill, ..... $64.37 .21,4$ !.rod Jiilh, : $\}$.at the first flag on red hill.Cooxum hill, Pernacoil hill, ... . 3854 56,4Station near Mooratan, 76 2603,1
: .. . . : . . atcoonem hile.
Permacoil hill,-Woxitty hill, . . . . 2722 55,91st flag on red hill, . $87.51 \quad 51,8$
 Fenteran: Oherved Angides.
1st fang ón xed $\}$ Station near Mroopatas, 91 45. 26,9 Chengciunt sta-
tion, $\}$
ditto, ... . 7609093
ATMYLUM station.
Permacoil hill ${ }_{j}$ Chengcaud station, . 129 95 52,8 Moaratan station, , 7309 50,7 Waritty hilh, . . . . 4621 11,4

## AT CHENGCAUD STATIOA.

Permacoil hill, Mylum station, . . $21.0426,9$ Mooratan station, . 5149 09,6

| $\begin{aligned} & \text { Trioandepoo- } \\ & \text { jū hill } \end{aligned}$ | ditto, . . . . 6608 35,2 |
| :---: | :---: |
| Cormum hind: | ditto, . . . 49 24 35,75 |

at the btation of observation at trivandePGORUM HILL.
Mooratan sta-
tion, . . : . Chengcaud station, $4908 \quad 59,9$
Referring light $\}$ Polar star, west elonnumbaucum, $\}$ gation,

Pebruary 3, . 1189 43,25

| 4, |  |  | 44,9 |
| :---: | :---: | :---: | :---: |
| 5, | $\cdot$ |  | 44,33 |
| 7, | $\cdots$ |  | 40,5 |
| 9, |  | 48,9 |  |
| 10, | $\cdots$ | 39,6 |  |
| 11, | $\cdots$ | $\cdots$ | 49,67 |

 Ma

The angles in general have been taken three and four times, and every time that the ohject was observed, both microscopes were tead off thrice, and two separate field books kept for making out the angles. What are here recorded, are the means taken from the two books. In case a difference in those angles, noticed at the time, left any reason to suspect an error in the instrument, the division. between the dots was carefully examined, as well as those to the tight and left, and if any error was discovered, allowance was made accordingly.

SECTION V. Trianales.
North. End of the Base from the South End of the Base 40006,4.

| No. | Stations. | Observed Angles. |  | Error. | Angles for calealation. | Distante in fee? |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | North end of the base, <br> South end of the base, Mount station, | $\bullet$ $\prime$ $\prime \prime$ <br> 91 09 04,0 <br> 11 19 32,5 <br> 77 31 23,0 <br> 179 59 59,5 <br> Mount station | $\begin{array}{\|l\|l\|} \hline 1 \cdots & \\ -, 03 & \\ -, 02 & \\ \hdashline, 03 & \\ \hline, 08 & , 08 \end{array}$ |  |  | $\begin{array}{r} \cdot \\ 8046,7 \\ 40965,8 \end{array}$ |
| 2. | North end of the base, South end of the base, Perumbauk. hill, | 0 , $\mu$ <br> 9 47 58,9 <br> 13 5 47,2 <br> 0 0 0 <br>    <br> umbauk hill f | $\begin{array}{c\|c\|} \hline \text { " } & \\ -, 01 & \\ -, 08 & \\ \text { from }\left\{\begin{array}{l} \text { Nort } \\ \text { Sout } \end{array}\right. \end{array}$ | th end th end | $\circ$ , $\prime \prime$  <br> 9 47 58,8  <br> 1 13 56 47,2 <br> 56 15 14  <br> 180,00 00   | $\begin{aligned} & \therefore \\ & \because \\ & 439718 \\ & 818903 \end{aligned}$ |

MERIDLAN ON THLE COASTOF COROMANDEL. 165
North ewd of the Base from Perumbauk Hill 49971,8.


It appears from examining the abowe triangles, that there is a difference in the distance from the north end of the base and Mount station, by the first and second triangles, and also a difference in the distance from the south end of the base to $P e$ rumbauk hill. It may be necessary to notice here, that there was great difficulty in taking all these angles, on account of the very thick vapour which constantly floated near the surface of the flat where the base line runs, almost immediately after daylight; to very near the time of sun-setting. All the angles, and particularly at the north and south end of-the base line, have been repeatedly taken, and the only time when the flag-staff appeared distinctly, was in the morning of the 7 th of October, -...... . M $\mathbf{M}$
when I obsetved the polar star at the south end of the base fine.

It was discovered, that at Perumbauk hill, there had been an error in reading off the south end of the base, most probably of $10^{\prime \prime}$ from the microme ${ }^{+}$ ters, as all the angles which had a reference to that point, exceeded what they ought to have been by ten or twelve seconds. In consequence of this disagretment, I chose to take the supplemental angle in the second and fourth triangles, after the other angles had been corrected. The distance of the north end of the base from Perumbaule, as determined in the second triangle, being taken as a base in the third triangle, wherein the three angles have been observed to determine the distance from $P a$ rumbauk to the Mount, and from the north end of the base to the Mount; it appoare that the latter distunce cothes out within 0,4 of a foot to what had 'been brought by the first triangle; and that the distance from the south end of the base to Porumbauk hitl derived from the second and fourth triangles, diter oigly, 14 of a foot. The distance from the Mount to Perumbauk being that fromwhich all the operations are to commence, I wished to be as pratticular as possibté in determining it, and the results from the third and foutth triangles make it 43495,4 and 43495,5, differing oly ontenth of a foot.

Mount ștation from Perumbauk Hill 43496,4.


## 

Prerumbauk Hili from Mungot station 59999,1.


## Perumbauk Hill from Mullapode Hill 65805,2.



Mullapode Hill from Conopwaucum Hill 47088,5.


Mullapode Hill from Mungot station 45109,5,

| No. | Stations. | Observed Angles. |  | Error. | Angles for calculation. | Distatces in feet. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9. | Mullepode hill; Mungot station, Munnoor station, | $\circ$ $\prime$ $\prime \prime$ <br> 81 10 56,8 <br> 49 14 29,4 <br> 49 34 32,4 <br> 179 59 38,6 <br> unnoor station |  |  |  | $\begin{aligned} & 44944,3 \\ & 58633,6 \end{aligned}$ |
| 10. | Mulapode hill, NAangot station, Tandray station, | $\|$$\bullet$ $\prime$ $\prime \prime$ <br> 28 17 36,7 <br> 124 40 24,2 <br> 27 02 00,1 <br> 180 0 01 <br> andray station | $\begin{array}{\|l\|l\|} \hline \prime \prime & \\ +, 04 \\ \hline, 6 \\ \hline, 1 & \\ \hline \vdots & \text { from }\left\{\begin{array}{l} \text { Mull } \\ \text { Mum } \end{array}\right. \\ \hline \end{array}$ | $\times, 8$ <br> apode ot sta | - $\prime$ $\prime \prime$ <br> 28 17 36,4 <br> 124 40 23,6 <br> 27 02 00 <br>    <br>    <br> hili,  - <br> tion, - - | 81731,9 <br> 47105,3 |
| Mullapode Hill from Munnoor station 44944,3. |  |  |  |  |  |  |
| 11. | Mullapode hill, Munnoor station, Tandray station, | 0 $\prime$ $\prime \prime$ <br> 52 53 20 <br> 93 -50 5,9 <br> 33 16 30,8 <br> 179 59 56,7 <br> ndray fation: - |  | -, 4 <br> llapode <br> nnoor s <br> -.. | 0 $\vdots$ 4 <br> 52 53 21 <br> 93 50 08 <br> 33 16 31 <br> 180   <br> hill, $\cdots$ $\vdots$ | $\begin{aligned} & 81732,7 \\ & 65325,7 \end{aligned}$ |

## MERIDIAN ON THE COAST, OP ROMOMANDEL. 169

Mungot station from Munnoor station 58633.7: :

| No. | Stations. | Observed Augles. | Diff. |  | Error. | Angles for calculation. | Distraces in feet. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12. | Mungot station, Munnoor station, Tandray station, | - ' " | " | 1 |  | - |  |
|  |  | $75 \quad 25$ 54,8 | -,3 |  |  | 7525 54,5 |  |
|  |  | 4415 34,9 | $-2$ |  |  | 44 13. 35. |  |
|  |  | 6018 30,7 | $-2^{2}$ |  |  | 601830,5 |  |
|  |  | 130,00 00,4 |  | ,64 | -', | $180 \quad \cdots:$ |  |
|  |  | dray station | frōin | $\left\{\begin{array}{l}M u \\ M u\end{array}\right.$ | ngot bill | tation, $-\cdots$ | 47105,9 65325,4 |

In the quadralateral formed by Mullapode hill, Mungot hill, Manmoor station, and Tandray station, the side Mullapode and Tandray is common to the tenth and eleventh triangles, the first of which gives it 817731,9 feet, and the latter 81739,7 feet, the mean of whigh is 81732,3 feet, which becomes the base for extending the triangles westerly. These results appear to be sufficiently correct, since the bases, on which the two triangles have been formed, were derived from the different sides of the triangle Perumbrak hill, Mungot hill, and Mrullapode hill, viz. one from the side Mullapode hill and Mungot hill, the other from the side Mudlapode hill and Perumbauk hill, on which was com=puted the side Mullapode hill and Coonorwaucum hill, and from that again the side Mullapode hill and Munnoor station, which, however, came out the same as when obtained from the distance Mul- . lapode hill and Mungot hill,

It will also appear that in the triangle computed on the base Mungot hill and Munnoor station, that each of the sides, Munnoor station and Tandray station, and Mungot and Tandray become common to the triangles, Mullapode hill, Munnoor and Tan-.
dray and Mullapode hill, Mungot and Tandiay, each to each, and that in the first case, there is a difference of $\frac{3}{10}$ and in the second of $\frac{6}{10}$. of a foot. These circumstances will, I conceive, prove the operations to be sufficiently satisfactory.

Mullapode hill ftom Tandray station 81732;s.

| No. | Stationa | Observed Angles. | Diff. |  | Earor. | Angles for calculation. | Distances: in feet. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13. |  | 0 7 $\alpha$ <br> -42 57 07,9 <br> 94 00 01,7 <br> 43, $d 2$ 60 <br> 193 59 59,6$\|$ <br> Inrumbaucdm | $7 \times 11$ <br> $-; 4$ <br> $-; 8$ <br> -4 | $1,6$ |  |  | $\left\|\begin{array}{c} i \\ \cdots \\ 119414,7 \\ 81587,1 \end{array}\right\|$ |
| 14. | Mullapode hill, Tandray station,' Peonark mallda, | $\left\{\begin{array}{ccc}0 & \prime & \prime \prime \\ 71 & 39 & 26,3 \\ 80 & 48 & 45,7 \\ 27 & 31 & 47,4 \\ \hline 179 & 59 & 59,4\end{array}\right.$ <br> Poonauk hill |  |  |  |  | 174555,7 167839,7 |

Poonauk hill from:Urrumbaucum hill 90399,4.


## MERIDHAN DN PHE COAET OF COMDMASHEL. 171

-Poonauk hill from Allicoor kill. 58638,4 .


## Manapode hitl.grom Urrmbauciom $119444 ;{ }^{\circ}$



Nhatupout Wity from Poonauk hill 174555:
 Maumdoor hill from Mullapode 138685,5.

| No. | Stations. | Observed <br> Angles. | Diff. | 遃突 | Error. | Angles for calculation. | $\begin{aligned} & \text { Distancess } \\ & \text { in feet. } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 19. | Maumdoor hiH, Mullapode hill, Carrangooly hill | $\begin{array}{\|ccc\|} \hline 0 & \prime & \prime \prime \\ 69 & 50 & 21,5 \\ 45, ~ 48 & 0,5 \\ 64 & 21 & 44,1 \end{array}$ | 1 $-1,2$ -1 $-1,2$ |  |  | $69.50-19,5$ 45 48 58,5 642148 |  |
|  |  | $180 \quad 6,1$ |  | 3,4 | +9,7 | 180 |  |
|  |  | angooly hill | from | Ma | umdoo <br> llapode |  | 110182,4 144405,4 |

Carrangooly hill from Maumdoor kill 110282,4.


Wooritty hill from Carrangooly tijll 9 sass, 8.


MERIDIAN ON THE COAST OF COROMANDEL. 173.
Carrangooly kill from Permocoil hill 194236,4.


## Permacoil hill from Vellungcaud hïl 88004,7.



## Wooritty hill from Permacoil hill 68041,5.



Permacoil Aitu from Coonum Adm 45150,5.


## Permacoil hill from Wooritty hill 68041,5.



Permacoil hill from Mylum station 49184,8.


## MERIDWAY OA SHE COAST OP COBOMANDEL. 175

Coonum hill from first Fílag on red hill 57567,7.

| isa | 8tatione. | Observid Anglis. | Diff | \% ${ }_{\text {co }}$ | Errot. | Angles for \&alculation. | Distances in feet. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 28. | Coonum hill, 1st Flag on red hill, Mooretanstations | $\begin{array}{ccc} 0 & 0 & \cdots \\ 0 & 0 & 0 \\ 76 & 26 & 03,1 \\ 81 & 48 & 30 \end{array}$ | $\begin{aligned} & -1 \\ & \rightarrow 1 \end{aligned}$ | $\cdots$ | $\cdots$ |  |  |
|  |  |  |  | 0,29 |  | $180 \quad 00$ |  |
|  |  | ara statio | rom | Coid | Flag | on red hill, | 5653, 5 21550,1 |

Permacoil Hill from the sere st ation of red hill 76334, 1.


Permacoil hill from Mooratan station 83350, 15.


Coonum hill from Mooratan station 56538,5.


Mooratan station from Chengcaud station 72253,8.


The angles have been taken with much care, and I believe with as much accuracy as the nature of such a process admits of; difficulty, however, very frequently arose from the haziness of the weather, which rendered the objects at the very distant points extremely dull, and occasioned some irregularity in the angles. Whenever that happened, the observations were often repeated, and in case any one, in particular, was different from the other so much as ten seconds, it was rejected till the three angles of the triangle had been observ-
1 ed. If the sum of these angles was near what it

## meridian on the coast of coromandel. 177

ought to be, no further notice was taken of it; but should the sum of the three angles be nearer the truth by taking it into the account, and that there appeared an irregularity in the other two observed angles, I have made it a rule to take each observed angle as a correct one, and divide the excess or defect between the other two, and then compute from the given side the other two sides; and after doing the same thing with each of the angles successively, a mean of the sides thus brought out was taken, which, to certain limits, will always be near the truth. I then varied the selection of the observed angles, rejecting such as I had reason to doubt; and by correcting them, and computing the two required sides of the triangle, those which gave the sides nearest to what had been brought out by the other method, were adopted, let the error be what it would. This, however, has rarely happened; and when it did, great precaution was used; and no angle was rejected without some reason appeared to render it doubtful.

In correcting the observed angles to obtain those made by the chords, I have used the formula given by the Astronomer Royal, in his demonstration of M. De Lambre's problem, which appears in the Philosophical Transactions for 1797. The spherical excess is of course had from the well known method of dividing the area of the triangle in square seconds, by the number of seconds in the arc equal to radius, where the number of feet in a second may be had by using the degree as has been commonly applied to the mean sphere, or the mean between the degree on the meridian and its. perpendicular. This being of no further use than to check any error that might happen in computing: the corrections for the angles.

In converting the sides of the triangles into atices, Vol. VIII.
the length of a degree has been computed for every ten degrees from the meridian to its perpendicular on an Ellipsoid, whose diameters were in the ratio of one to 1,0067 , which is derived from taking the degree on the meridian, in latitude $50^{\circ} 41^{\prime}$ to be 60851 , and the degree perpendicular thereto 61182 , in the same latitude. These data would give the meridional degree, in latitude $13^{\circ}$, to be 60191, and the degree perpendicular equal 60957, which, however, is pot the case; but no sensible error will arrive in making those corrections from taking the arcs a few seconds more or less than the truth.

## SECTION VI,

Reduction of the distances to the meridian of Trivandeporum, for determining the length of the terrestrial arci.
The sides of the great triangles, from which the arc is derived, falling very nearly in the same meridian, and not more than 16363,3 feet west from the meridian of Trivandeporim, the south extremity of the arc, there required no reference to any hypothesis of the earth's figure for getting the exact distance between the parallels, so that the latitude of a point where a great circle falling from the station of observation near Paudree, will cut the meridiạn of Trioandeporum at right angles, may be determineed with sufficient accuracy by computing spherically, and the distances, when reduced to the meridian, (the distance from Trivandeporum to Coonum hill excepted,) may be considered as the chords of arcs on the meridian, and therefore the arcs themselves may be had, by allowing 60494 fathoms to the degree, as had been obtained from the sum of those reduced distances, the sum therefore of all these arcs will make the whole merin dional are, which is a nearer approximation to the truth.

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Seeing that a line drawn from the station of observation at Paudree, to the station at Maumdoor hill, would fall nearly in the direction of the meridian, that distance has been computed, by taking the sides Poonauk hill to Maumdoor hill, and Poonauk hill to Padree, and using the internal angle at Poonauk hill, corrected for the chords. This, however, was scarcely necessary, except for shewing the arrangement of the points.

The following table will shew the arrangement of the sides, and their reduction to the meridian of Trivandeporum.

| Stations at | Stations referred to. | Bearings referred tothe meridian of Tri-vandeporwom. | Distances. | Distances from the parallels of the |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Meridian. | Perpendicnlar. |
| Trioandeporum, | Coonum hill, | 531 50,3.N.W. | 125129,1 | 12059,8 W. | 124547,5 N. |
| Coonum hill, | Wooritty hill, | 00318,4 N.W. | 104887,5 | 108,3 W. | 104887,4 N. |
| Wooritty hill, | Carrangooly, | 5245 21,9 | 95282,8 | 75851,4 E. | 57666,0 N. |
|  | Maumdoor, | 150 51,2 N.W. | 133481,5 | 4303,5 W. | 133412,5 N. |
| Maumdoor, | Paudree station, | 10209,7 N. E. | 211512,1 | $3824,4 \mathrm{E}$. | 211477,5 N. |

THE NORTHINGS REDUCED TO ARCS.
Trivandeporum to Coonum hill, . . 124548,77
Coonum hill to Wooritty hill, . 104887,47
Wooritty hill to Maumdoor hill, . 13341s,15
Maumdoor hill to Paudree station, 211478,57
Length of the terrestrial arc, . . . 574327,96
Or fathoms, . . . . . . . . . . . . 95721,3266

## SECTION VII.

Observations by the Zenith Sector for the latitude of Paudree station, and the station near Trivandeporum; and the length of the celestial arc.
The zenith sector, with which these observations have been taken, was made by Mr. Ramsden, and is the one alluded to by General Roy, in the Philosophical Transactions for 1790, being then unfinished. The radius of the arc is five feet, and the arc itself is of that extent to take in nine degrees on each side of the zenith. It is divided into degrees, and smaller divisions of $20^{\prime}$ each, which are numbered. Each of these last is again subdivided into four, of $5^{\prime}$ each. The micrometer which moves the telescope and arc, is graduated to seconds, and one revolution moves the arc over $1^{\prime} 10^{\prime \prime} 08^{\prime \prime \prime}$, but the scale being large, a small fraction of a second can be easily defined. The construction, and improvements to the zenith sector, are so well known, that a minute description of it here would be unnecessary. It will therefore suffice to say, that as far as so delicate an instrument can be managed in a portable observatory, or travelling ${ }^{\circ}$ tent, which never can offer the advantages of a fixed, well contrived building, I have every reason to be satisfied with it.

The time I commenced observing at Paudree station was during the heavy part of the monsoon, which occasioned frequent interruptions: and although I had intended observing by at least three fixed stars, I only succeeded to my satisfaction in one, which was Aldebaran. With that star I had a fortunate succession for about sixteen nights; some few of those observations being less favourable than the others, were rejected, and the rest, from which the latitude was determined, appear in the following table,arranged in the order in which they were taken.

MERIDIAN ON THE COAST OF COROMANDEL. 18:
During the time I was at Trivandeporum, near Cuddalore, the weather was settled and serene, and the nights perfectly clear, so that I had an unlimited choice of stars, but having been successful with Aldebaran, I chose that star for determining the length of the arc.

As I consider the celestial arc more likely to be erroneous than any terrestrial measurement, I have thought it. necessary to give some account of the manner of observing and of adjusting the instrument, for after two years experience, I have found, that notwithstanding the great powers of the zenith sector, extreme delicacy and attention are requisite to render the observations satisfactory. The following method of adjustment I have always practised. After having brought the vertical axis nearly to its true position by the adjusting screw at the bottom, or, so that the wire of the plummet would bisect the same dot when the telescope was moved to the opposite side, or half round on the axis, I then examined whether the dot at the centre of the horizontal axis was bisected, and whether the wire moved in the vertical plane clear of the the axis; for unless it be perfectly free, all the observations will be false. When I had bisected the dot, I either took out the microscope and looked obliquely, or did the same by a magnifying glass, and by that means I could discover the smallest parallax. If it admitted being brought nearer to the axis, it was done; but I found from experience, that it was more eligible to leave the wire at a sensible distance than to bring it very near. Having satisfied myself in this particular, I examined with the microscope again in front, moved the wire freely in the vertical plane, and then bisected the dot. The telescope was then moved, so that: the wire was brought over the dot zero on the arc, and the same precaution used with respect to the wire mov-
ing free of the arc; and here, as well as above, 1 found it best to allow' a sensible distance between the wire and the arc.

The microscope by which the upper dot in the horizontal axis is examined, being fixed by the maker, the axis of vision is of course at right angles to the vertical plane, and will meet that plane in the centre of the axis, but the lower microscope is moveable, and requires care to fix it so.as to have the wire in the axis of vision, and be free from the effects of parallax, this I have done by moving it along the brass plate in front of the arc, till the wire appeared free from curvature, and then adjusted the dot. In these late observations, I have generally made the final adjustment by the light of a wax taper, for the wind being sometimes high and troublesome, I found there was much irregularity in the observations, until I adopted that method. I therefore closed the doors and windows of the observatory tent, so as to have a perfect stillnesi within. The distance of the wire from the axis and the arc is likewise better defined by a taper by noticing the shadow in moving the light to the right and left.

In fixing the instrument for the star, great care was taken to have it placed in the meridian, which was done by a mark at near the distance of a mile, (generally one of my small flags), the polar star, having been previously observed by the large theodolite for that purpose. The telescope was then moved in the vertical till the wire of the plummet was at the nearest division on either limb- to the zenith distance of the star, which could always be nearly known. The micrometer, having been put to zero, was firmly serewed, and the dot on the limb carefully bisected, the instrument was turned half round; the adjustment examined and correet-
ed, if necessaty. That being done, the degrees and minutes, \&ic. on the arc were noted down; as was also the particular division on the micrometer scale, at which the index stood; and the fractional part of a division in case threfe were ary. In this' state every thing remained to within fifteen or twenty minutes of the time the star was to pass, when I repaired to the tent, and again examined whether the wire bisected the dot; if it did not, the instrument was again adjusted to the same dot, and the horizontal axis also examined by the uppermicroscope, all this being done, the sector was placed in the meridian.

When the star entered the field of view, the micrometer was moved gently till the star was near the horizontal wire, but not bisected till if came near the vertical, that the micrometer might not be turned back, but continue moving in the same direction. This I did to avoid any false motion: in the micrometer screw, and I was led to this precaution by the repeated experiments I had made in examining the divisions on the arc, for it sometimes happened after moving the arc over one of the divisions till the wire bisected the next dot; and then turning it back again, that the index of the micrometer was not at the same second, but had passed over it perhaps one, and sometimes two seconds ; but by moving over the next five minutes in the same direction, the number of revolutions: and seconds were atways what they ought to be, to some very small fraction. This anomaly, how-' ever, only happened in some situations of the screw, and to avoid any errors arising therefrom, I adopted the above method.

The zenith distance of the star being now had, on one part of the arc or limb, after the same procese had been gone through the next night, with regard to the adjustment, the zenith distance was
taken on the other part of the arc, by turning the instrument half round on its vertical axis. The mean of these two was therefore the true observed zenith distance, and half the difference was the error of collimation. For applying these to the ${ }_{s}$ purpose in question, the mean of the zenith distances being corrected for refraction, the declination of the star for each of these nights, was corrected for nutation, aberration, \&c. to the time of observation, and the mean of the two taken for determining the latitude.

In this manner has the whole series of observations been continued, by turning the sector half round every night, for the purpose of observing on opposite parts of the arc, and each compared with its preceding and succeeding one. In pursuing this method, it was unnecessary to notice the error of ${ }^{-}$ collimation for any other purpose than as a test to the regularity of the observations; for until they became uniform, no notice was taken of the zenith distances, concluding that there had been some mismanagement, or some defect in the adjustment.

The following tables contain the observations by the star Aldebaran, for determining the length of the arc.

Observations at the station near Paudree.

| Day of the month. | Mean of the ze nith distance on each arc. | Mean of the corrected declinations. | Latitude. |
| :---: | :---: | :---: | :---: |
|  | - ' " | - " " | - , |
| Noo. 23d and 24th, | 24632,5 | 1606 20,70 | 1319 48,20 |
| - 24th and 25th, | $24632,4{ }^{2}$ | 160620,69 | 131948,83 |
| 25th and 26th, | 24631,78 | 160620,68 | 1319 48,90 |
| 30th and 1st Dec. | 24631,60 | 160620,61 | 1319 49,01 |
| Dec. 1st and 2d, | 24632,60 | 160620,60 | 1319 48,0 |
| 2d and 3d, | 24632,90 | 160620,58 | 1319 47,68 |
| 12 th and 13th, | 24630,96 | 160620,39 | 131949,43 |
| 13th and 14th, | 24628,57 | 160620,36 | $13 \quad 19 \quad 51,79$ |
| $\left.\begin{array}{l} \text { Error of col- } \\ \text { Lima. applied. } \end{array}\right\} 27 \text { th, }$ | 24629,71 | 160619,64 | 1319 49,93 |
| Mean 1319 49,018 |  |  |  |

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Observations at the station near Trivandeporum.

| Day of the month. | Mean of the zemith distance on each arc. | Mean of the correct declinations. | Latitude. |
| :---: | :---: | :---: | :---: |
|  | - ' " | - " | - 1 |
| February 10th and 11th, | 42127,14 | 1606 18,00 | 114450,86 |
| 11th and 13th, | 421 24,04 | 1606 17,93 | 114453,89 |
| 13th and 14th, | 42123,04 | $16.0617,87$ | 114454,83 |
| 14 th and 15th, | 42125,10 | 160617,83 | 114452,73 |
| 15 th and 16th, | 42126,73 | 160617,79 | 114451,06 |
| 16 th and 17th, | 42125,60 | 160617,75 | 114452,15 |
| 24th and 25th, | 42124,17 | 1606 17,44 | 114453,27 |
| 25th and 26th, | 42125,17 | $1606 \quad 17,40$ | 114452,23 |
| 26th and 27th, | , 42125,04 | $1606 \quad 17,37$ | 114452,33 |
| Mean 114458,59 |  |  |  |

Latitude of the station near Paudree 1319 49,02$\left.\begin{array}{c}\text { Latitude of the station near Tri- } \\ \text { vandeporum . . . . .. . . . . . }\end{array}\right\} 114452,59$

## Difference of latitude, nearly. 134 56,43

The latitude of a point where a great circle passing through Paudree station, and cutting the imeridian of Trivandeporum at right angles, will be $13^{\circ} 19^{\prime} 49^{\prime \prime}, 02-$, from which deduct the latitude of the station at 7 rivandeporum, equal $11^{\circ} 49^{\prime} 52^{\prime \prime}, 59$, will leave $1^{\circ} 34^{\prime} 56^{\prime \prime}, 43$, or $1^{\circ}, 58233$ nearly; by which divide the number of fathoms in the terrestrial arc $=95721,3266, \& c$. we shall have $1^{\circ}=$ 60494 fathoms, nearly, for the degree in the middle of the arc, or latitude $12^{\circ} 39^{\prime}$ nearly.

## APPENDIX.

Since the account of the meridional arc was made out, I have completed the measurement of a degree perpendicular to the meridian in latitude $12^{\circ}$ $32^{\prime}$ nearly, which is derived from a distance of fifty-five miles and upwards, between Carangooly and Curnatighur; two stations nearly east and
west from each other; and the following triangles have been made use of to obtain that distãnce.

Distance, Carangooly from Permacoil 134236,4.


Carangooly from Maillacherry Droog 208418,2.


The distance from Curnatighur to Maillacherry. has also been brought out from a northern series of triangles derived from the side of Poonauk hill and Maumdoor hill, of the great triangle Maumdoor, Poonauk, and Mullapode hill: the triangles are Poonauk, Maumdoor and Hanandamulla; Hanandamulla, Maumdoor, and Telloor; Telloor; Hanandamulla and Curnatighur; Curnatighur, Telloor and Maillacherry Droog. Upon the distance from Curnatighur to Maillacherry as a base, the distance from Curnatightur to Carangooly has been computed, and differs only two feet from that derived from the side Carangooly and Maillacherry Droog: but there was some variation in the angles taken at Poonauk hill, which renders it doubtful, for the present, which to select; I have therefore relied on the single distance given in the thirtyfourth triangle.

Of the Polar Star Observations at Carangooly and Curnatighur, ando the Length of a Degree, perpendicular to the Meridian, deduced therefrom, for the Latitude of $12^{\circ} 32^{\prime}$ nearly.
As the method of determining the difference of longitude of two places, by taking the angle with the meridian and each station reciprocally, requires very great accuracy, I have thought it necessary to give an account of the obsetvations for that purpose, and to state at the same time, the difficulty of taking them, particularly at Curnatigur, whose great height subjected it to a constant haziness, whereby the blue lights at Carangooly were repeatedly fired without effect, appearing'too faint to be seen when the wires of the telescope were illuminated: some nights, however, were favourable, when the whole of the lights were distinctly seen; but the anxiety, which occurs on such occasions, will sometimes cause irregularities in the angles; a few on that account, when the lights expired before the observations were thought sufficiently satisfactory, have been rejected. Those which appear in the following account, are such as I have deemed good, though there is a greater difference among them thran I could have wished. But as I had no positive reason forsetting them aside, I have accordingly used them; and have endeavoured to lessen the error, by increasing the number of observations, at Ca rangooly, between the polar star, at its greatest western elongation, and the referring lamp at Saldawauk.


Between the Lamp at Sallawauk and the Blue Light at Curnatighur.

| March 30, | $\ldots 84^{\circ}$ | $38^{\prime}$ |
| :---: | :---: | :---: |
| April | 24,0 |  |
| 4, | $\ldots$. | 23,55 |
|  | $\ldots$. | 19,2 |
|  |  | 20,0 |
|  |  | 22,62 |

Mean . . . . . . $84^{\circ} 38^{\prime} 21^{\prime \prime}, 87$
TABLE. Containing the apparent Polar Distances of the Star, and the apparent Azimuths for the Nights of Observation; and also the Angles between the referring Lamp and the Meridian of Carangooly.

| $\begin{aligned} & \text { March } \\ & 1803 . \end{aligned}$ | Apparent Polar dist. | Latitude. | Apparent Azimuth. | $\mid \angle \text { Star and }$ | $\angle$ Pole and Lamp. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 14422,32 | f | 14655,32 | 03448,4 | 22143,72 |
| 21 | 14422,62 |  | 14655,63 | 03452,9 | 22148,53 |
| 22 | 14422,88 |  | 14655,90 | 03452,8 | 22148,70 |
| 23 | 14423,16 |  | 14656,18 | 034 48,8 | 22144,98 |
| 25 | $1 \begin{aligned} & 1 \\ & 44 \\ & 23,71\end{aligned}$ | $\left\{\begin{array}{lll}12^{\circ} & 32^{\prime} & 12 \\ \end{array}\right.$ | 14656,72 | 034 50,2 | 22146,92 |
| 26 | 14424,01 |  | 1 46 57,05 | 084 48,0 | 22145,05 |
| 27 | $1 \begin{array}{lll}1 & 44 & 24,28\end{array}$ |  | 14657,33 | 03446,9 | 221 44,23 |
| 29 | $\mid 14424,82$ |  | 146 57,89 | 034 45,4 | 221 43,29 |
| Observed angle between the lamp and Curnatighur, -8438 21,87Observed angle meridian of Carangooly and ditto, $-\quad-8700$ 07;54 |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |

Observations at Curnatighur, between the Polar Star, at its greatest eastern Elongation, and the referring Lamp at Maudimungalum.
May 14, in the morning, . . . $82^{\circ} 26^{\prime} 25^{\prime \prime}, 6$
15, . . . . . . . . . . . . 25,2
16, ............. 25,6
20, . . . . . . . . . . . 28,29
21,
26,1

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Between the referring Light and the Blue Lights at Carangooly.

| May 18, | $8^{\circ} 35^{\prime} 34^{\prime \prime}, 50$ |
| :---: | :---: |
|  | 36,30 |
|  | 40,10 |
|  | 42,0 |
|  | 41,25 |
|  | 38,20 |
|  | 35,57 |
|  | 38,40 |

$$
\text { Mean . . . . , } 835 \text { 38,26 }
$$

TABLE. Containing the apparent Polar Distances of the Star, the apparent Azimuths for the Time of Observation, and also the Angles between the referring Lamp and the Meridian of Curnatighur.


If the mean of all the angles be taken, the observed angle at Carangooly, between the meridian and Curnatighur, will be $87^{\circ} 00^{\prime} 07^{\prime \prime}, 54$; and the observed angle at Curnatighur, between that meridian and the station at Carangooly, will be $92^{\circ} 49^{\prime}$ 15",93. In order, therefore, to correct these angles. for spherical computation, it will first be necessary to ascertain the distance between the parallels of Carangooly and Curnatighir, so that the one being known, the other may be obtained.

Let $P C$ and $P G$ be two meridians, and let $C$ and $G$ be the stations at Carangooly and Curnatighur. Let $C$ s be a parallel of latitude at $C$, meeting the meridian of Curnatighur produced, and let $C R$ be a great circle perpendicular to the meridian of Carangooly falling from that place, till it meet $P G$ produced in $R$.

Now GCR is a spheroidical triangle, and the chord of the arc $G C$ is given from the thirtyfourth triangle; and since the angle $P G C$ is known, the angle $C G R$ is known, being equal $180^{\circ}$ minus the observed angle at Curnatighur, or $87^{\circ} 10^{\prime} 44^{\prime \prime}, 07$.-And by the same reasoning the angle $G C R$ will be given, being equal the angle $P C R$ ( $90^{\circ}$ ) minus the observed angle at Ca - $\boldsymbol{R}$
 rangooly, that is $2^{\circ}$ $59^{\prime} 52^{\prime \prime}, 46$-Hence, by first considering this as a plane triangle, and taking the angle at $R$, the supplement to the, other two, the sides $C R$ and $\boldsymbol{G} \boldsymbol{R}$ may be obtained, and used as arcs for correcting the angles at $C$ and $G$, which will then be $2^{\circ} 59^{\circ} 52^{\prime \prime}, 2$ and $87^{\circ} 10^{\prime} 43^{\prime \prime}, 79$ respectively, which are the angles made by the chords of the arcs $C G$ and $R G$ at $C$ and $G$. Hence the supplement to these ( $89^{\circ} 49^{\prime} 24^{\prime \prime}, 01$ ) will be the angle at $R$ made by the chords of the arcs $R C$ and $R G$. From these data will be had $R C=290837,8$, and $R G=$ 15228,74 feet.

But to find the small space $R \mathrm{~s}$ on the meridian of Curnatighur, between the perpendicular arc and parallel from Carangooly, let the triangle CRs be taken as a plane one. Then if to the corrected angle $C R \mathrm{~s}\left(89^{\circ} 49^{\prime} 24^{\prime \prime}, 01\right)$ be added the supplement to the spherical excess in the triangle $R C G$ ( $0^{\prime \prime}, 5$ ), we shall have $89^{\circ} 49^{\prime} 24^{\prime \prime}, 51$ for the angle $s R C$. Draw $R t$ parallel to $s C$, meeting the meridian of Carangooly, produced in $t$. Then since the angles $P t R$ and $P_{s} C$ are equal by construction; and the triangles $\mathrm{s} C R, C R t$ considered as plane ones, the angle $C R t$ is equal half the difference of the angles $P C R$ and $P R C$, that is $=$ $\frac{20^{\circ}-\left(80^{\circ} 99^{\circ}-24 ", 51\right)}{0^{\prime \prime}}=0^{\circ} 5^{\prime} 17^{\prime \prime}, 74$. Hence is given the two angles $C R \mathrm{~s}, \mathrm{~s} C R$, and the side $C R$, by which the small side $R$ s is had, equal to 448,08 feet, which, deducted from $G R$, gives $G_{\mathrm{s}}=$ 14780,72 feet, equal to an arc of $2^{\prime} 26^{\prime \prime}, 58$ on the meridian, and this is the difference of the latitudes of Carangooly and Curnatighur. Hence if the latitude of *Carangooly be $12^{\circ} 39^{\prime} 12^{\prime \prime}, 27$, that of Curnatighur will be $12^{\circ} 34^{\prime} 38^{\prime \prime}, 85$, and their respective complements will be $77^{\circ} 27^{\prime} 47^{\prime \prime}, 73$ and $77^{\circ} 25^{\prime} 21^{\prime \prime}, 15$. Hence in the triangle $P C G$, on the spheroid, is given the two sides $P G$ and $P C$, the co-latitudes of $G$ and $C$, and the two observed angles $P C G$ and $P G C$.

Then as the tan. $77^{\circ} 26^{\prime} 34^{\prime \prime}, 44$ (half the sum of the sides $P G$ and $P C$ ) to tan. $0^{\circ} 1^{\prime} 13^{\prime \prime}, 29$ (half their difference) so is tan. $89^{\circ} 54^{\prime} 41^{\prime \prime}, 73$ (half the sum of the angles), to tan. $2^{\circ} 56^{\prime \prime} 10^{\prime \prime}, 23$ (the half

[^0]difference of the angles). Therefore $92^{\circ} 50^{\prime} 51^{\prime \prime}, 96$ and $86^{\circ} 58^{\prime} 31^{\prime \prime}, 5$, will be the angles at Curnatighur and Carangooly, 'such as would have been observed on a sphere, the latitudes and longitudes being the same. Then by using these angles, with the sides $P C$ and $P G$, and computing spherically, the angle $C P G$, or difference-of longitude, will be $48^{\prime} 47^{\prime \prime}, 75$, with which, and the side $P C$, or co-latitude of Carangooly, in the triangle $P C R$, right angled at $C$, the side $C R$ will be had equal $0^{\circ} 47^{\prime} 37^{\prime \prime}, 45$.

Now the chord of this arc is the distance $\boldsymbol{C R}$, equal 290837,8 feet, and therefore the arc itself is 290841 feet nearly. Hence $47^{\prime} 37^{\prime \prime}, 45$ : 290841 :: $60^{\prime}: 366355,08$ feet, or 61059,2 fathoms nearly, which is the length of the degree perpendicular to the meridian at Carangooly*.
ridian be 60494 fathoms; by using these data, and computing on the elliptic hypothesis, the degree perpendicular to the meridian $12^{\circ} 32^{\prime \prime}$ would be 60906 fathoms, which for the present purpose is made use of.

By the triangles, the point $O$ is east from the meridian of Trivandeporum 190561,12 feet, and north from the perpendicular at that station 480563,62 feet. Also $\boldsymbol{C}$ is east 63690,8 feet, and north 287100,96 feet, from which, and applying the above degrees, we shall have the arc TM $1^{\circ} 19^{\prime} 26^{\prime \prime}, 4$; $\boldsymbol{T} m=47^{\prime} 27^{\prime \prime}, 56$; and therefore $=\mathbf{M m} 31^{\prime}$ $58^{\prime \prime}, 84$. Also $O M 31^{\prime} 17^{\prime \prime}, 13, C m=10^{\prime}$ $27^{\prime \prime}, 42$, and $P O 76^{\circ} 55^{\prime} 56^{\prime \prime}, 7$, the latitude of the observatory being $13^{\circ} 04^{\prime} 09^{\prime \prime}, 3$.

Then in the spherical triangle POM, right angled at $M$, we have $\operatorname{Cos} O M$ : Rad $::$ Cos. PO: $\operatorname{Cos} P M=76^{\circ} 55^{\prime} 48^{\prime \prime}, 72$, to which add the arc $M m$, there will be had $P m=77^{\circ} 27^{\prime} 47^{\prime \prime}, 56$, the co-latitude of the point $m$.

Then again as rad. : $\operatorname{Cos} \operatorname{Cm}:=\operatorname{Cos} m P$ :
 $\operatorname{Cos} P C=77^{\circ} 27^{\prime} 47^{\prime}, 77$; therefore the latitude of Carangooly, will be $12^{\circ} 32^{\prime} 12^{\prime \prime}, 23$.
*The ratio of the earth's diameters has been determined, by using the degree as brought'out here, and the one in latitude $50^{\circ}$ 41', as deduced from the measured arc between Greenwich and Paris, which is 60851 fathoms; and these two give the ratio of the polar to the equatrial diameters to be $1: 1,003567$, supposinge the earth to be an ellinsoid.

## POSTSCRIPT.

Since the above has been written, the triangles derived from the side Maumdoor and Poonauk, and brought down westerly as far as Woritty, have been computed, and it appears that the distance between Maumdoor and Woritty, which is common to both series, exceeds the former by 6,9 feet; so that the mean of the two, equal 133485,0 feet, has been taken for obtaining anew both the meridional and perpendicular arcs; the former of which is 574337,04 feet, and the latter 290848,5 feet; whence the degree on the meridian will be had 60495 fathoms nearly, and the degree perpendicular to the meridian at Carangooly 61061 fathoms nearly.

The difference of 6,9 feet is more than what I expected, but it has been occasioned by the great difficulty in getting the angles in the great triangle, Maumdoor, Mullapode, and Poonauk. But as it appears that the side Mullapode and Maumdoor has been in excess, and the side Poonauk and Maumdoor in defect, it musi follow that the mean distance of Maumdoor and Woritty, brought out by triangles derived from these two sides, must be very near the truth.

Now this latitude has been made use of to find the latitude of Curnatighur, and the same process has been followed for finding the length of a degree on the perpendicular in the latitude of Carangooly as is here given; and that degree taken, with the easting of the observatory from the meridian of Carangaoly to compute the latitude a second time, which came out $12^{\circ} 32^{\prime} 12^{\prime \prime}, 27$, and is here applied for re-computing the perpendicular degree: but the difference is too trifling to affect the difference of longitude, and therefore the degree comes out the same.

It is scarcely necessary to notice, that the distance of the observatory from the meridian of Trivándepoorum being so trifling, no spheroidal correction has beeu thought requisite for obtaining the latitude of the point $M$, and much less for that of $C$.

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$\therefore$ -
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[^0]:    * When the polar star observations were made at Carangooly, no double aximuths could be taken, and therefore the latitude of the place was necessary to compute the azimuths, in order to get the direction of the meridian. As I wished to deduce the latitude of Carangooly from that of the observatory at Madras, the follewing method was used to obtain it.

    Let $\boldsymbol{P}$ be the pole, $\boldsymbol{P T}$ the meridian of Trivandeporum, $\mathbf{O}$ the observatory at-Madras; and let $\boldsymbol{C}$ be the station at Carangooly, Tthat at Trivandeporum, $O M$ an arc of a great circle; perpendicular to PT, falling from the observatory, and Cm another perpendicular arc from Carangooly. Then if the ratio of the earth's diameters be taken as 1 to 1,003567 , and the degree on the me-

